

Numerical Analysis &
Computer Programming

Previous year Questions from
2017 to 1992

Ramanasri Institute

2017

1. Explain the main steps of the Gauss-Jordan method and apply this method to find the inverse of the matrix $\begin{bmatrix} 2 & 6 & 6 \\ 2 & 8 & 6 \\ 2 & 6 & 8 \end{bmatrix}$. [10 Marks]
2. Write the Boolean expression $z(y+z)(x+y+z)$ in the simplest form using Boolean postulate rules. Mention the rules used during simplification. Verify your result by constructing the truth table for the given expression and for its simplest form. [10 Marks]
3. For given equidistant values u_{-1}, u_0, u_1 and u_2 a values is interpolated by Lagrange's formula. Show that it may be written in the form $u_x = yu_0 + \frac{y(y^2-1)}{3!}\Delta^2 u_{-1} + \frac{x(x^2-1)}{3!}\Delta^2 u_0$, where $x+y=1$. [15 Marks]
4. Derive the formula $\int_a^b y dx = \frac{3h}{8}[(y_0 + y_n) + 3(y_1 + y_2 + y_4 + y_5 + \dots + y_{n-1}) + 2(y_3 + y_6 + y_{n-3})]$. Is there any restriction on n ? State that condition. What is the error bounded in the case of Simpson's $\frac{3}{8}$ rule? [20 Marks]
5. Write an algorithm in the form of a flow chart for Newton-Raphson method. Describe the cases of failure of this method. [15 Marks]

2016

6. (i) 4096 (ii) 0.4375 (iii) 2048.0625
Convert the following decimal numbers to univalent binary and hexadecimal numbers: (10 marks)
7. Let $f(x) = e^{2x} \cos 3x$ for $x \in [0,1]$. Estimate the value of $f(0.5)$ Using Lagrange interpolating polynomial of degree 3 over the nodes $x=0, x=0.3, x=0.6$ and $x=1$. Also compute the error bound over the interval $[0,1]$ and the actual error $E(0.5)$ (20 marks)
8. For an integral $\int_{-1}^1 f(x) dx$ show that the two point Gauss quadrature rule is given by $\int_{-1}^1 f(x) dx = f\left(\frac{1}{\sqrt{3}}\right) + f\left(-\frac{1}{\sqrt{3}}\right)$ using this rule estimate $\int_2^4 2xe^x dx$ (15 marks)
9. Let A, B, C be Boolean variable denote complement $\bar{A}, \bar{A} + B$ of is an expression for $A \text{ OR } B$ and $\bar{B}. A$ is an expression for $\bar{A} \text{ AND } B$. Then simplify the following expression and draw a block diagram of the simplified expression using AND and OR gates.
 $A.(A+B.C).(\bar{A}+B+C).(A+\bar{B}+C).(A+B+\bar{C})$. (15 marks)

2015

10. Find the principal (or canonical) disjunctive normal form in three variables p, q, r for the Boolean expression $((p \wedge q) \rightarrow r) \vee ((p \wedge q) \rightarrow \bar{r})$. Is the given Boolean expression a contradiction or a tautology? (10 Marks)
11. Find the Lagrange interpolating polynomial that fits the following data:

x	-1	2	3	4
$f(x)$	-1	11	31	69

Find $f(1.5)$

(20 Marks)

12. Solve the initial value problem $\frac{dy}{dx} = x(y-x)$, $y(2) = 3$ in the interval $[2, 2.4]$ using the Runge-

Kutta fourth-order method with step size $h = 0.2$

(15 Marks)

13. Find the solution of the system

$$10x_1 - 2x_2 - x_3 - x_4 = 3$$

$$-2x_1 + 10x_2 - x_3 - x_4 = 15$$

$$-x_1 - x_2 + 10x_3 - 2x_4 = 27$$

$$-x_1 - x_2 - 2x_3 + 10x_4 = -9$$

using Gauss-Seidel method (make four iterations)

(15 Marks)

2014

14. Apply Newton-Raphson method to determine a root of the equation $\cos x - xe^x = 0$ correct up to four decimal places.

(10 Marks)

15. Use five subintervals to integrate $\int_0^1 \frac{dx}{1+x^2}$ using trapezoidal rule.

(10 Marks)

16. Use only AND and OR logic gates to construct a logic circuit for the Boolean expression $z = xy + uv$

(10 Marks)

17. Solve the system of equations

$$2x_1 - x_2 = 7$$

$$-x_1 + 2x_2 - x_3 = 1$$

$$-x_2 + 2x_3 = 1$$

using Gauss-Seidel iteration method (perform three iterations)

(15 Marks)

18. Use Runge-Kutta formula of fourth order to find the value of y at $x = 0.8$, where $\frac{dy}{dx} = \sqrt{x+y}$, $y(0.4) = 0.41$. Take the step length $h = 0.2$

(20 Marks)

19. Draw a flowchart for Simpson's one-third rule.

(15 Marks)

20. For any Boolean variables x and y , show that $x + xy = x$.

(15 Marks)

2013

21. In an examination, the number of students who obtained marks between certain limits were given in the following table:

Marks	30-40	40-50	50-60	60-70	70-80
No. of students	31	42	51	35	31

Using Newton forward interpolation formula, find the number of students whose marks lie between 45 and 50. **(10 Marks)**

22. Develop an algorithm for Newton-Raphson method to solve $f(x) = 0$ starting with initial iterate x_0 , n be the number of iterations allowed, epsilon be the prescribed relative error and delta be the prescribed lower bound for $f'(x)$ **(20 Marks)**

23. Use Euler's method with step size $h = 0.15$ to compute the approximate value of $y(0.6)$, correct up to five decimal places from the initial value problem. $y' = x(y + x) - 1$, $y(0) = 2$ **(15 Marks)**

24. The velocity of a train which starts from rest is given in the following table. The time is in minutes and velocity is in km/hour.

t	2	4	6	8	10	12	14	16	18	20
v	16	28.8	40	46.4	51.2	32.0	17.6	8	3.2	0

Estimate approximately the total distance run in 30 minutes by using composite Simpson's $\frac{1}{3}$ rule. **(15 Marks)**

2012

25. Use Newton-Raphson method to find the real root of the equation $3x = \cos x + 1$ correct to four decimal places **(12 Marks)**

26. Provide a computer algorithm to solve an ordinary differential equation $\frac{dy}{dx} = f(x, y)$ in the interval $[a, b]$ for n number of discrete points, where the initial value is $y(a) = \alpha$, using Euler's method. **(15 Marks)**

27. Solve the following system of simultaneous equations, using Gauss-Seidel iterative method : **(20 Marks)**

$$3x + 20y - z = -18$$

$$20x + y - 2z = 17$$

$$2x - 3y + 20z = 25$$

28. Find $\frac{dy}{dx}$ at $x = 0.1$ from the following data: **(20 Marks)**

x :	0.1	0.2	0.3	0.4
y :	0.9975	0.9900	0.9776	0.9604

29. In a certain examination, a candidate has to appear for one major & two major subjects. The rules for declaration of results are marks for major are denoted by M_1 and for minors by M_2 and M_3 . If the candidate obtains 75% and above marks in each of the three subjects, the candidate is declared to have passed the examination in first class with distinction. If the candidate obtains 60% and above marks in each of the three subjects, the candidate is declared to have passed the examination in first class. If the candidate obtains 50% or above in major, 40% or above in each of the two minors and an average of 50% or above in all the three subjects put together, the candidate is declared to have passed the examination in second class. All those candidates, who have obtained 50% and above in major and 40% or above in minor, are declared to have passed the examination. If the candidate obtains less than 50% in major or less than 40% in anyone of the two minors, the candidate is declared to have failed in the examinations. Draw a flow chart to declare the results for the above. **(20 Marks)**

2011

30. Calculate $\int_2^{10} \frac{dx}{1+x}$ (up to 3 places of decimal) by dividing the range into 8 equal parts by Simpson's $\frac{1}{3}$ rule. (12 Marks)
31. (i) Compute $(3205)_{10}$ to the base 8.
 (ii) Let A be an arbitrary but fixed Boolean algebra with operations \wedge, \vee and $'$ and the zero and the unit element denoted by 0 and 1 respectively. Let x, y, z, \dots be elements of A . If $x, y \in A$ be such that $x \wedge y = 0$ and $x \vee y = 1$ then prove that $y = x'$... (12 Marks)
32. A solid of revolution is formed by rotating about the x -axis, the area between the x -axis, the line $x = 0$ and $x = 1$ and a curve through the points with the following co-ordinates:
- | | | | | | |
|-----|------|--------|--------|--------|--------|
| x | 0.00 | 0.25 | 0.50 | 0.75 | 1 |
| y | 1 | 0.9896 | 0.9589 | 0.9089 | 0.8415 |
- Find the volume of the solid. (20 Marks)
33. Find the logic circuit that represents the following Boolean function. Find also an equivalent simpler circuit:
- | x | y | z | $f(x, y, z)$ |
|-----|-----|-----|--------------|
| 1 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 |
- (20 Marks)
34. Draw a flow chart for Lagrange's interpolation formula. (20 Marks)

2010

35. Find the positive root of the equation $10xe^{-x^2} - 1 = 0$ correct up to 6 decimal places by using Newton-Raphson method. Carry out computations only for three iterations. (12 Marks)
36. (i) Suppose a computer spends 60 per cent of its time handling a particular type of computation when running a given program and its manufacturers make a change that improves its performance on that type of computation by a factor of 10. If the program takes 100 sec to execute, what will its execution time be after the change?
 (ii) If $A \oplus B = AB' + A'B$, find the value of $x \oplus y \oplus z$. (6+6=12 Marks)
37. Given the system of equations
- $$2x + 3y = 1$$
- $$2x + 4y + z = 2$$
- $$2y + 6z + Aw = 4$$
- $$4z + Bw = C$$

State the solvability and uniqueness conditions for the system. Give the solution when it exists. **(20 Marks)**

38. Find the value of the integral $\int_1^5 \log_{10} x \, dx$ by using Simpson's $\frac{1}{3}$ rd rule correct up to 4 decimal places. Take 8 subintervals in your computation. **(20 Marks)**

39. (i) Find the hexadecimal equivalent of the decimal number $(587632)_{10}$
 (ii) For the given set of data points $(x_1, f(x_1), (x_2, f(x_2), \dots, (x_n, f(x_n))$ write an algorithm to find the value of $f(x)$ by using Lagrange's interpolation formula
 (iii) Using Boolean algebra, simplify the following expressions
 (a) $a + a'b + a'b'c + a'b'c'd + \dots$
 (b) $x'y'z + yz + xz$ where x' represents the complement of x **(5+10+5=15 Marks)**

2009

40. (i) The equation $x^2 + ax + b = 0$ has two real roots α and β . Show that the iterative method given by: $x_{k+1} = -\frac{(ax_k + b)}{x_k}, k = 0, 1, 2, \dots$ is convergent near $x = \alpha$, if $|\alpha| > |\beta|$

(ii) Find the values of two valued Boolean variables A, B, C, D by solving the following simultaneous equations:

$$\bar{A} + AB = 0$$

$$AB + AC$$

$$AB + A\bar{C} + CD = \bar{C}D$$

where \bar{x} represents the complement of x

(6+6=12 Marks)

41. (i) Realize the following expressions by using NAND gates only :

$$g = (\bar{a} + \bar{b} + c)\bar{d}(\bar{a} + e)f$$

(ii) Find the decimal equivalent of $(357.32)_8$ **(6+6=12 Marks)**

42. Develop an algorithm for Regula-Falsi method to find a root of $f(x) = 0$ starting with two initial iterates x_0 and x_1 to the root such that $\text{sign}(f(x_0)) \neq \text{sign}(f(x_1))$. Take n as the maximum number of iterations allowed and epsilon be the prescribed error. **(30 Marks)**

43. Using Lagrange interpolation formula, calculate the value of $f(3)$ from the following table of values of x and $f(x)$:

x	0	1	2	4	5	6
$f(x)$	1	14	15	5	6	19

(15 Marks)

44. Find the value of $y(1.2)$ using Runge-Kutta fourth order method with step size $h = 0.2$ from the initial value problem: $y' = xy, y(1) = 2$ **(15 Marks)**

2008

45. Find the smallest positive root of equation $xe^x - \cos x = 0$ using Regula-Falsi method. Do three iterations. **(12 Marks)**

46. State the principle of duality

- (i) in Boolean algebra and give the dual of the Boolean expressions $(X + Y) \cdot (\overline{X} \cdot \overline{Z}) \cdot (Y + Z)$ and $X\overline{X} = 0$
- (ii) Represent $(\overline{A} + \overline{B} + \overline{C})(A + \overline{B} + C)(A + B + \overline{C})$ in NOR to NOR logic network.

(6+6=12 Marks)

47. (i) The following values of the function $f(x) = \sin x + \cos x$ are given:

x	10°	20°	30°
$f(x)$	1.1585	1.2817	1.3360

Construct the quadratic interpolating polynomial that fits the data. Hence calculate $f\left(\frac{\pi}{12}\right)$.

Compare with exact value.

- (ii) Apply Gauss-Seidel method to calculate x, y, z from the system:

$$-x - y + 6z = 42$$

$$6x - y - z = 11.33$$

$$-x + 6y - z = 32$$

with initial values $(4.67, 7.62, 9.05)$. Carry out computations for two iterations

(15+15=30 Marks)

48. Draw a flow chart for solving equation $F(x) = 0$ correct to five decimal places by Newton-Raphson method

(30 Marks)

2007

49. Use the method of false position to find a real root of $x^3 - 5x - 7 = 0$ lying between 2 and 3 and correct to 3 places of decimals.

(12 Marks)

50. Convert:

(i) 46655 given to be in the decimal system into one in base 6.

(ii) $(11110.01)_2$ into a number in the decimal system.

(6+6=12 Marks)

51. (i) Find from the following table, the area bounded by the x -axis and the curve $y = f(x)$ between $x = 5.34$ and $x = 5.40$ using the trapezoidal rule:

x	5.34	5.35	5.36	5.37	5.38	5.39	5.40
$f(x)$	1.82	1.85	1.86	1.90	1.95	1.97	2.00

(15 Marks)

- (ii) Apply the second order Runge-Kutta method to find an approximate value of y at $x = 0.2$ taking $h = 0.1$, given that y satisfies the differential equation and the initial condition

$$y' = x + y, y(0) = 1$$

(15 Marks)

2006

52. Evaluate $I = \int_0^1 e^{-x^2} dx$ by the Simpson's rule

$$\int_a^b f(x) dx \approx \frac{\Delta x}{3} [f(x_0) + 4f(x_1) + 2f(x_2)] + 4f(x_3) + \dots + 2f(x_{2n-2}) + 4f(x_{2n-1}) + f(x_{2n})]$$
 with

$$2n = 10, \Delta x = 0.1, x_0 = 0, x_1 = 0.1, \dots, x_{10} = 1.0$$

(12 Marks)

53. (i) Given the number 59.625 in decimal system. Write its binary equivalent.

(ii) Given the number 3898 in decimal system. Write its equivalent in system base 8.

(6+6=12 Marks)

54. If Q is a polynomial with simple roots $\alpha_1, \alpha_2, \dots, \alpha_n$ and if P is a polynomial of degree $< n$, show that

$$\frac{P(x)}{Q(x)} = \sum_{k=1}^n \frac{P(\alpha_k)}{Q'(\alpha_k)(x - \alpha_k)}$$

Hence prove that there exists a unique polynomial of degree with given values c_k at the point α_k , $k = 1, 2, \dots, n$.

(30 Marks)

55. Draw a flowchart and algorithm for solving the following system of 3 linear equations in 3

$$\text{unknowns } x_1, x_2 \text{ \& } x_3 : C * X = D \text{ with } C = (c_{ij})_{i,j=1}^3, X = (x_j)_{j=1}^3, D = (d_i)_{i=1}^3$$

(30 Marks)

2005

56. Use appropriate quadrature formulae out of the Trapezoidal and Simpson's rules to numerically

integrate $\int_0^1 \frac{dx}{1+x^2}$ with $h = 0.2$. Hence obtain an approximate value of π . Justify the use of

particular quadrature formula.

(12 Marks)

57. Find the hexadecimal equivalent of $(41819)_{10}$ and decimal equivalent of $(111011.10)_2$ (12 Marks)

58. Find the unique polynomial $P(x)$ of degree 2 or less such that $P(1) = 1, P(3) = 27, P(4) = 64$. Using the Lagrange's interpolation formula and the Newton's divided difference formula, evaluate $P(1.5)$

(30 Marks)

59. Draw a flow chart and also write algorithm to find one real root of the non linear equation $x = \phi(x)$ by the fixed point iteration method. Illustrate it to find one real root, correct up to four places of decimals, of $x^3 - 2x - 5 = 0$.

(30 Marks)

2004

60. The velocity of a particle at distance from a pint on it s path is given by the following table:

$S(\text{meters})$	0	10	20	30	40	50	60
$V(\text{m/sec})$	47	58	64	65	61	52	38

Estimate the time taken to travel the first 60 meters using Simpson's $\frac{1}{3}$ rd rule. Compare the result

with Simpson's $\frac{3}{8}$ th rule.

(12 Marks)

61. (i) If $(AB, CD)_{16} = (x)_2 = (y)_8 = (z)_{10}$ then find x, y & z

(ii) In a 4-bit representation, what is the value of 1111 in signed integer form, unsigned integer form, signed 1's complement form and signed 2's complement form? (6+6=12 Marks)

62. How many positive and negative roots of the equation $e^x - 5 \sin x = 0$ exist? Find the smallest positive root correct to 3 decimals, using Newton-Raphson method. (10 Marks)

63. Using Gauss-Siedel iterative method, find the solution of the following system:

$$4x - y + 8z = 26$$

$$5x + 2y - z = 6 \quad \text{up to three iterations.}$$

$$x - 10y + 2z = -13$$

(15 Marks)

2003

64. Evaluate $\int_0^1 e^{-x^2} dx$ by employing three points Gaussian quadrature formula, finding the required weights and residues. Use five decimal places for computation. **(12 Marks)**
65. (i) Convert the following binary number into octal and hexa decimal system:
101110010.10010
- (ii) Find the multiplication of the following binary numbers: 11001.1 and 101.1 **(6+6=12 Marks)**
66. Find the positive root of the equation $2e^{-x} = \frac{1}{x+2} + \frac{1}{x+1}$ using Newton-Raphson method correct to four decimal places. Also show that the following scheme has error of second order:
$$x_{n+1} = \frac{1}{2} x_n \left(1 + \frac{a}{x_n^2} \right)$$
 (30 Marks)
67. Draw a flow chart and algorithm for Simpson's $\frac{1}{3}$ rd rule for integration $\int_a^b \frac{1}{1+x^2} dx$ correct to 10^{-6} **(30 Marks)**

2002

68. Find a real root of the equation $f(x) = x^3 - 2x - 5 = 0$ by the method of false position. **(12 Marks)**
69. (i) Convert $(100.85)_{10}$ into its binary equivalent.
- (ii) Multiply the binary numbers $(1111.01)_2$ and $(1101.11)_2$ and check with its decimal equivalent **(4+8=12 Marks)**
70. (i) Find the cubic polynomial which takes the following values:
 $y(0) = 1, y(1) = 0, y(2) = 1$ & $y(3) = 10$. Hence, or otherwise, obtain $y(4)$
- (ii) Given: $\frac{dy}{dx} = y - x$ where $y(0) = 2$, using the Runge-Kutta fourth order method, find $y(0.1)$ and $y(0.2)$. Compare the approximate solution with its exact solution. ($e^{0.1} = 1.10517, e^{0.2} = 1.2214$). **(10+20=30 Marks)**
71. Draw a flow chart to examine whether a given number is a prime. **(10 Marks)**

2001

72. Show that the truncation error associated with linear interpolation of $f(x)$, using ordinates at x_0 and x_1 with $x_0 \leq x \leq x_1$ is not larger in magnitude than $\frac{1}{8} M_2 (x_1 - x_0)^2$ where $M_2 = \max |f''(x)|$ in $x_0 \leq x \leq x_1$. Hence show that if $f(x) = \frac{2}{\sqrt{\pi}} \int_0^{\pi} e^{-t^2} dt$, the truncation error corresponding to linear interpolation of $f(x)$ in $x_0 \leq x \leq x_1$ cannot exceed $\frac{(x_1 - x_0)^2}{2\sqrt{2\pi e}}$. **(12 Marks)**

73. (i) Given $A.B' + A'.B = C$ show that $A.C' + A'.C = B$
 (ii) Express the area of the triangle having sides of lengths $6\sqrt{2}$, 12 , $6\sqrt{2}$ units in binary number system. **(6+6=12 Marks)**

74. Using Gauss Seidel iterative method and the starting solution $x_1 = x_2 = x_3 = 0$, determine the solution of the following system of equations in two iterations

$$10x_1 - x_2 - x_3 = 8$$

$$x_1 + 10x_2 + x_3 = 12.$$

$$x_1 - x_2 + 10x_3 = 10$$

Compare the approximate solution with the exact solution **(30 Marks)**

75. Find the values of the two-valued variables A, B, C & D by solving the set of simultaneous equations

$$A' + A.B = 0$$

$$A.B = A.C$$

$$A.B + A.C' + C.D = C'.D$$

(15 Marks)

2000

76. (i) Using Newton-Raphson method, show that the iteration formula for finding the reciprocal of the p^{th} root of N is $x_{i+1} = \frac{x_i(p+1-Nx_i)}{p}$

- (ii) Prove De Morgan's Theorem $(p+q)' = p'.q'$ **(6+6=12 Marks)**

77. (i) Evaluate $\int_0^1 \frac{dx}{1+x^2}$, by subdividing the interval $(0, 1)$ into 6 equal parts and using Simpson's one-

third rule. Hence find the value of π and actual error, correct to five places of decimals

- (ii) Solve the following system of linear equations, using Gauss-elimination method:

$$x_1 + 6x_2 + 3x_3 = 6$$

$$2x_1 + 3x_2 + 3x_3 = 117$$

$$4x_1 + x_2 + 2x_3 = 283$$

(15+15=30 Marks)

1999

78. Obtain the Simpson's rule for the integral $I = \int_a^b f(x)dx$ and show that this rule is exact for polynomials of degree $n \leq 3$. In general show that the error of approximation for Simpson's rule is given by

$$R = -\frac{(b-a)^5}{2880} f^{iv}(\eta), \quad \eta \in (0,2).$$

- Apply this rule to the integral $\int_0^1 \frac{dx}{1+x}$ and show that $|R| \leq 0.008333$. **(20 Marks)**

79. Using fourth order classical Runge-Kutta method for the initial value problem $\frac{du}{dt} = -2tu^2, u(0) = 1$, with $h = 0.2$ on the interval $[0, 1]$, calculate $u(0.4)$ correct to six places of decimal. **(20 Marks)**

1998

80. Evaluate $\int_1^3 \frac{dx}{x}$ by Simpson's rule with 4 strips. Determine the error by direct integration. **(20 Marks)**
81. By the fourth order Runge-Kutta method. tabulate the solution of the differential equation $\frac{dy}{dx} = \frac{xy+1}{10y^2+4}$, $y(0) = 0$ in $[0, 0.4]$ with step length 0.1 correct to five places of decimals **(20 Marks)**
82. Use Regula-Falsi method to show that the real root of $x \log_{10} x - 1.2 = 0$ lies between 3 and 2.740646 **(20 Marks)**

1997

83. Apply that fourth order Runge-Kutta method to find a value of y correct to four places of decimals at $x = 0.2$, when $y' = \frac{dy}{dx} = x + y$, $y(0) = 1$ **(20 Marks)**
84. Show that the iteration formula for finding the reciprocal of N is $x_{n+1} = x_n(2 - Nx_n)$, $n = 0, 1, \dots$ **(20 Marks)**
85. Obtain the cubic spline approximation for the function given in the tabular form below:

x	0	1	2	3
$f(x)$	1	2	33	244

 and $M_0 = 0, M_3 = 0$ **(20 Marks)**

1996

86. Describe Newton-Raphson method for finding the solutions of the equation $f(x) = 0$ and show that the method has a quadratic convergence. **(20 Marks)**
87. The following are the measurements t made on a curve recorded by the oscillograph representing a change of current i due to a change in the conditions of an electric current:

t	1.2	2.0	2.5	3.0
i	1.36	0.58	0.34	0.20

Applying an appropriate formula interpolate for the value of i when $t = 1.6$ **(20 Marks)**
88. Solve the system of differential equations $\frac{dy}{dx} = xz + 1$, $\frac{dz}{dx} = -xy$ for $x = 0.3$ given that $y = 0$ and $z = 1$ when $x = 0$, using Runge-Kutta method of order four **(20 Marks)**

1995

89. Find the positive root of $\log_e x = \cos x$ nearest to five places of decimal by Newton-Raphson method. **(20 Marks)**
90. Find the value of $\int_{1.6}^{3.4} f(x) dx$ from the following data using Simpson's $\frac{3}{8}$ rule for the interval $(1.6, 2.2)$ and $\frac{1}{8}$ rule for $(2.2, 3.4)$:

x	1.6	1.8	2.0	2.2	2.4
$f(x)$	4.953	6.050	7.389	9.025	11.023

x	2.6	2.8	3.0	3.2	3.4
$f(x)$	13.464	16.445	20.086	24.533	29.964

(20 Marks)

1994

91. Find the positive root of the equation $e^x = 1 + x + \frac{x^2}{2} + \frac{x^3}{6} e^{0.3x}$ correct to five decimal places.

(20 Marks)

92. Fit the following four points by the cubic splines.

i	0	1	2	3
x_i	1	2	3	4
y_i	1	5	11	8

Use the end conditions Use the end conditions $y''_0 = y''_3 = 0$

Hence compute (i) $y(1.5)$

(ii) $y'(2)$

(20 Marks)

93. Find the derivative of $f(x)$ at $x = 0.4$ from the following table:

x	0.1	0.2	0.3	0.4
$y = f(x)$	1.10517	1.22140	1.34986	1.49182

(20 Marks)

1993

94. Find correct to 3 decimal places the two positive roots of $2e^x - 3x^2 = 2.5644$

(20 Marks)

95. Evaluate approximately $\int_{-3}^3 x^4 dx$ Simpson's rule by taking seven equidistant ordinates. Compare it with the value obtained by using the trapezoidal rule and with exact value.

(20 Marks)

96. Solve $\frac{dy}{dx} = xy$ for $x = 1.4$ by Runge-Kutta method, initially $x = 1, y = 2$ (Take $h = 0.2$)

(20 Marks)

1992

97. Compute to 4 decimal placed by using Newton-Raphson method, the real root of $x^2 + 4 \sin x = 0$.

(20 Marks)

98. Solve by Runge-Kutta method $\frac{dy}{dx} = x + y$ with the initial conditions $x_0 = 0, y_0 = 1$ correct up to 4 decimal places, by evaluating up to second increment of y (Take $h = 0.1$)

(20 Marks)

99. Fit the natural cubic spline for the data.

$x: 0 \ 1 \ 2 \ 3 \ 4$
 $y: 0 \ 0 \ 1 \ 0 \ 0$

(20 Marks)

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